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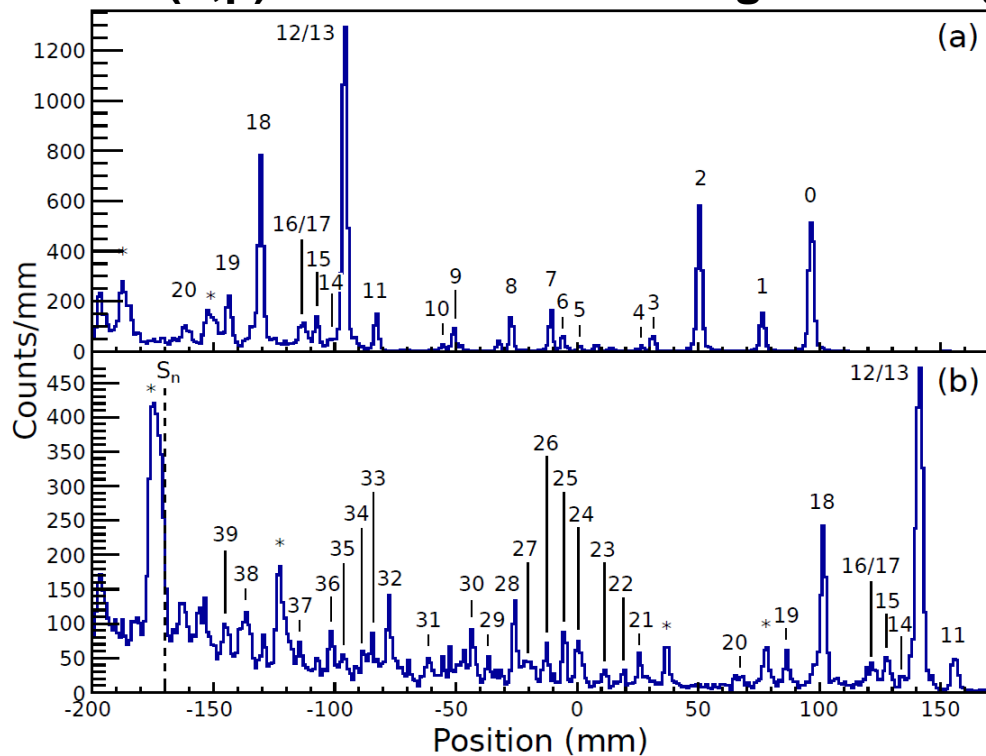
# Single-neutron strength in $N=29$ isotones: Subshell closures and missing $vg_{9/2}$ strength

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NSF Site Visit, John D. Fox Laboratory, Florida State University

# $N=29$ isotones via the $(d,p)$ reaction with the SE-SPS

$^{54}\text{Fe}(d,p)^{55}\text{Fe}$  16 MeV Lab angle = 30 deg



$^{50}\text{Ti}(d,p)^{51}\text{Ti}$  REU w/Ursinus (2019)

$^{54}\text{Fe}(d,p)^{55}\text{Fe}$  REU w/Ursinus (2021)

$^{51}\text{V}(d,p)^{52}\text{V}$  I. Hay Senior Thesis (2022)

$^{52}\text{Cr}(d,p)^{53}\text{Cr}$  REU w/Ursinus (2022)



# $N=29$ isotones via the $(d,p)$ reaction with the SE-SPS



PHYSICAL REVIEW C **103**, 064309 (2021)

## $^{50}\text{Ti}(d,p)^{51}\text{Ti}$ : Single-neutron energies in the $N = 29$ isotones, and the $N = 32$ subshell closure

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PHYSICAL REVIEW C **108**, 044306 (2023)

## $g_{9/2}$ neutron strength in the $N = 29$ isotones and the $^{52}\text{Cr}(d,p)^{53}\text{Cr}$ reaction

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PHYSICAL REVIEW C **106**, 064308 (2022)

## $^{54}\text{Fe}(d,p)^{55}\text{Fe}$ and the evolution of single neutron energies in the $N = 29$ isotones

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PHYSICAL REVIEW C **109**, 024302 (2024)

## Measurement of $g_{9/2}$ strength in the stretched $8^-$ state and other negative parity states via the $^{51}\text{V}(d,p)^{52}\text{V}$ reaction

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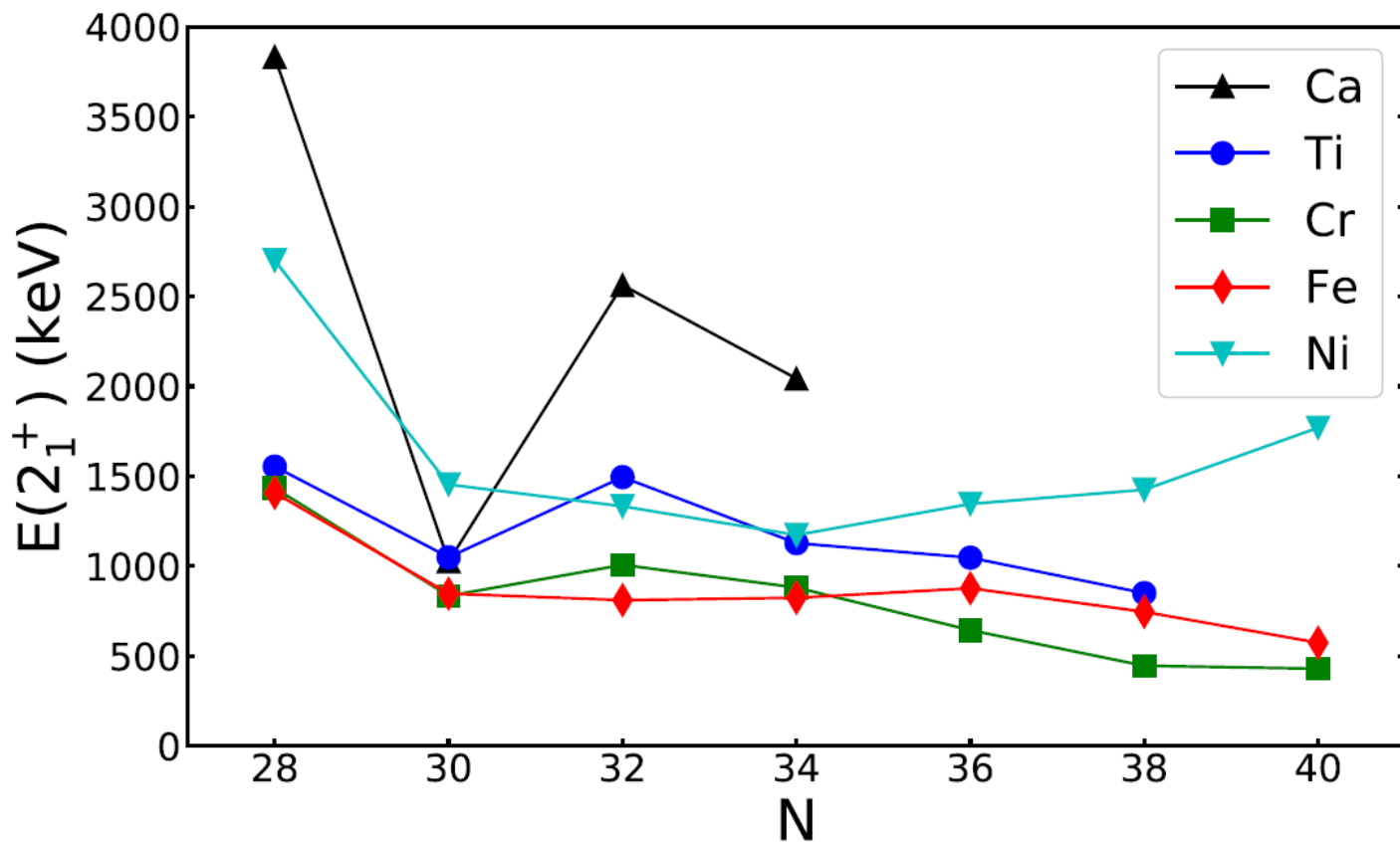
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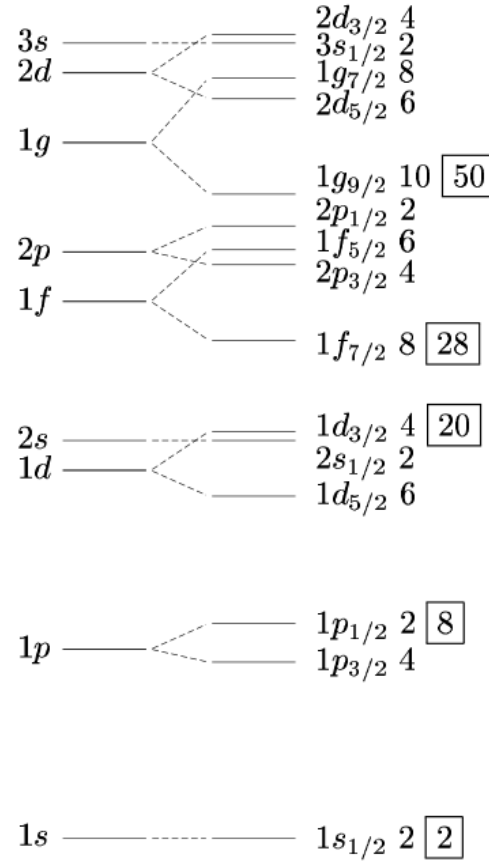


# *fp* orbits and the $N=32$ subshell closure

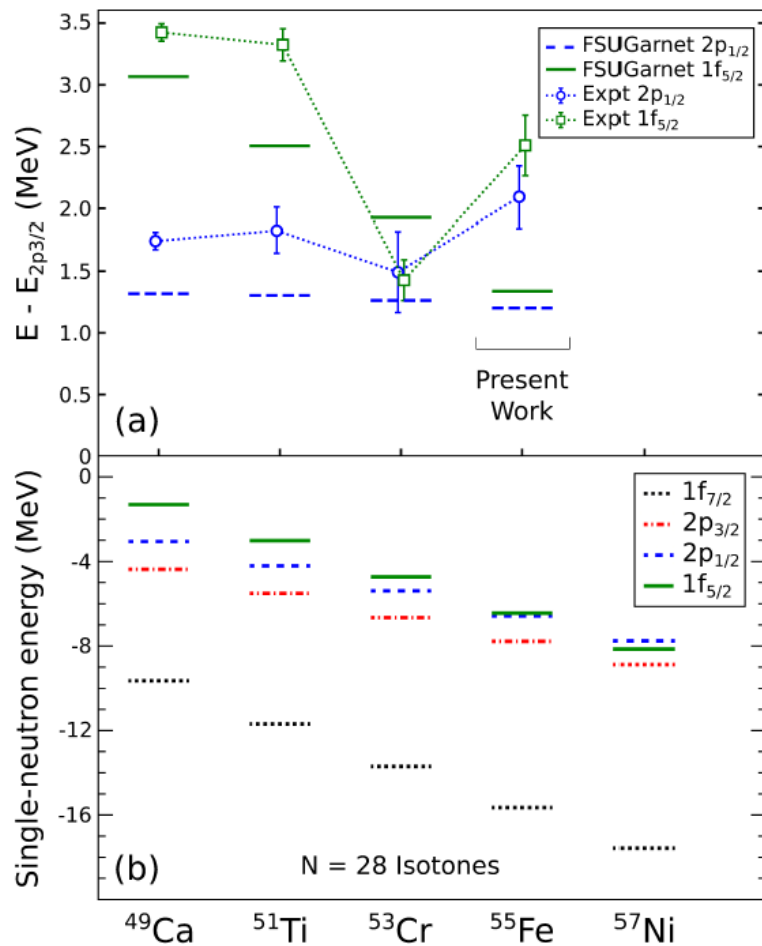




# $fp$ orbits and the $N=32$ subshell closure



# *fp* orbits and the $N=32$ subshell closure



$^{49}\text{Ca}$ : Y. Uozumi *et al.*, Nucl. Phys. A 576, 123 (1994).

$^{51}\text{Ti}$ : L.A. Riley *et al.*, Phys. Rev. C 103, 064309 (2021).

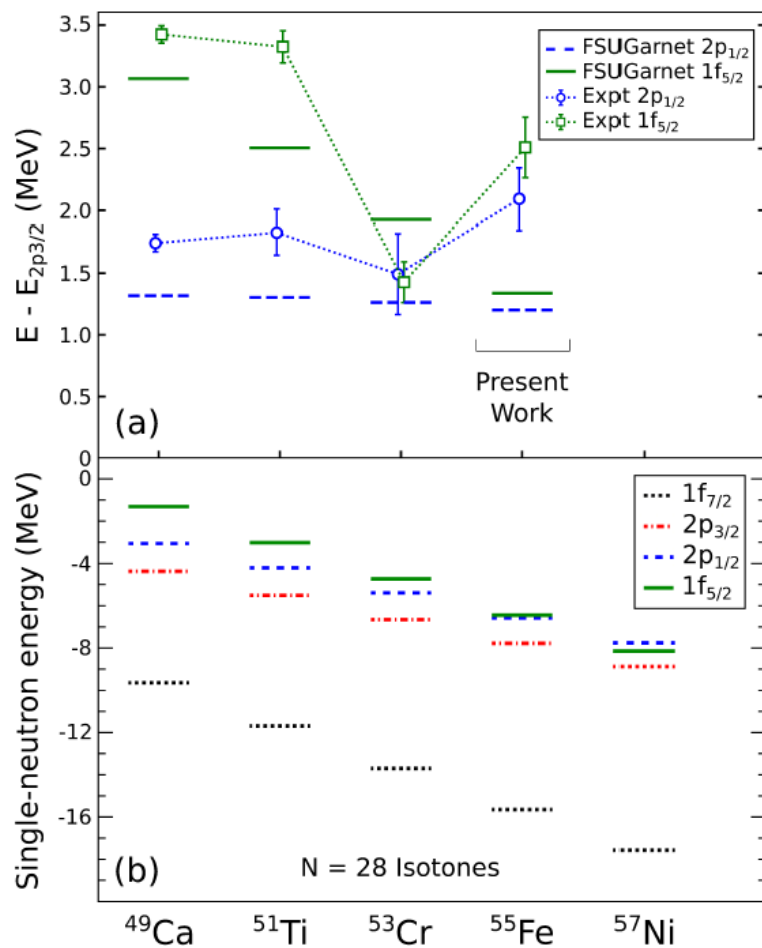
$^{53}\text{Cr}$ : H. Junde, Nucl. Data Sheets 110, 2689 (2009).

$^{55}\text{Fe}$ : L.A. Riley *et al.*, Phys. Rev. C 106, 064308 (2022).

Theory: J. Piekarewicz, Covariant Density Functional Theory calculations with the FSUGarnet covariant energy density functional



# *fp* orbits and the $N=32$ subshell closure



Analysis of  $^{52}\text{Cr}(d,p\gamma)^{53}\text{Cr}$  underway (L.A. Riley *et al.* at Ursinus College) to try to untangle  $p_{3/2}$  from  $p_{1/2}$  and  $f_{5/2}$  from  $f_{7/2}$  to improve *fp* single neutron energies.





# *fp* orbits and the $N=32$ subshell closure

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PHYSICS LETTERS

2 September 1968

## THE INFLUENCE OF $2p$ - $1h$ CONFIGURATIONS ON THE LOW-LYING STATES OF $^{51}\text{Ti}$

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Received 24 July 1968

Experimental evidence for  $2p$ - $1h$  configurations in  $^{51}\text{Ti}$  is obtained from study of the reaction  $^{49}\text{Ti}(t,p)^{51}\text{Ti}$ . To account for the relative intensities of the  $(t,p)$  transitions such configurations need to be included in shell-model calculations.

As part of a programme linking  $(t,p)$  and  $(d,p)$  studies to the same final nucleus we have examined odd- $A$  nuclei with one neutron beyond closed shells or sub-shells e.g.  $^{27}\text{Mg}$  [1],  $^{51}\text{Ti}$ ,  $^{59}\text{Fe}$  [2] and  $^{89}\text{Sr}$  [3]. Two-nucleon transfer reactions like the  $(t,p)$  reaction may be expected to excite configurations other than those seen in the  $(d,p)$  reaction and hence provide a more exacting test of theoretical calculations.

For  $N=29$  nuclei shell-model calculations [e.g. 4] are based on configurations obtained by coupling the odd neutron in either the  $2p_{3/2}$ ,  $2p_{1/2}$  or  $1f_{7/2}$  orbit to the even parity states of the proton core. A fair description of the level positions below  $\approx 3$  MeV excitation and of the spectroscopic factors observed in  $(d,p)$  reactions is then obtained providing one accepts agreement between

Table 1  
 $^{51}\text{Ti}$  data from the  $^{49}\text{Ti}(t,p)$  and  $^{50}\text{Ti}(d,p)$  reactions.

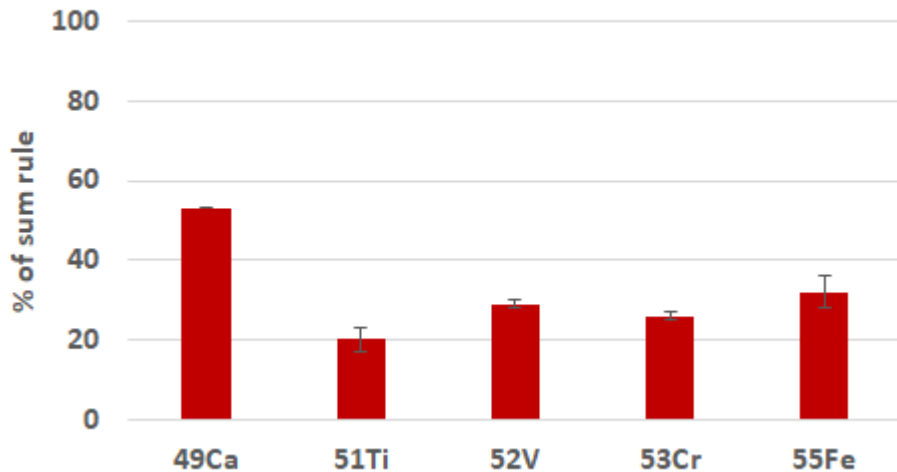
$E_x$	$J^\pi$	$L$	(t,p) Rel. Int.		
			Expt	Theory	Expt $S(d,p)$
0	$3/2^+$	2	1.0	1.0	0.82
1.16	$1/2^+$	4	0.10	0.35	0.59
1.43	$3/2^+$	0	1.38	-	0.075
1.56	$1/2^+$	2	0.62	0.09	0.04
2.14	$3/2^+$	2	0.12	0.003	0.28
2.19	$1/2^+$	2	0.23	0.34	0.06
2.69	$3/2^+$	0	26.0	-	0.01
2.90	$1/2^+$	4	0.25	0.41	0.34

Use  $^{49}\text{Ti}(t,p)$  reaction to distinguish between  $5/2^-$  and  $7/2^-$  states in  $^{51}\text{Ti}$



# $\nu g_{9/2}$ strength observed in N=29 isotones

Summed  $g_{9/2}$  strength observed in (d,p)



$^{49}\text{Ca}$ : Y. Uozumi *et al.*, Nucl. Phys. A 576, 123 (1994).

$^{51}\text{Ti}$ : L.A. Riley *et al.*, Phys. Rev. C 103, 064309 (2021).

$^{52}\text{V}$ : I.C.S. Hay *et al.*, Phys. Rev. C 109, 024302 (2024).

$^{53}\text{Cr}$ : L.A. Riley *et al.*, Phys. Rev. C 108, 044306 (2023).

$^{55}\text{Fe}$ : L.A. Riley *et al.*, Phys. Rev. C 106, 064308 (2022).



# $vg_{9/2}$ strength observed in N=29 isotones

## Open questions:

- 1) Are we using the right sum rule?

Kay, Schiffer and Freeman [Phys. Rev. Lett. 111, 042502 (2013)]:

Spectroscopic strengths quenched by short-range correlations between nucleons, as in  $(e,e'p)$ . Maximum spectroscopic strength is  $55 \pm 10\%$  of that expected from mean field theory.

John Millener (private communication during the last few weeks):

Calculations of  $1\hbar\omega$  excitations introduce spurious states. Sum rule must correct for this.

***Even with these caveats, we still may be missing  $vg_{9/2}$  strength.***



# $vg_{9/2}$ strength observed in N=29 isotones

## More open questions:

2) Is there a substantial amount of  $vg_{9/2}$  strength above the particle thresholds?

Piekarewicz Covariant Density Functional Theory calculations say that  $vg_{9/2}$  unbound in  $^{48}\text{Ca}$ ,  $^{50}\text{Ti}$  and  $^{52}\text{Cr}$ ; bound by only 1.4 MeV in  $^{54}\text{Fe}$ .

3) Are we missing a substantial amount of  $vg_{9/2}$  strength distributed among many bound states?





# $vg_{9/2}$ strength observed in N=29 isotones

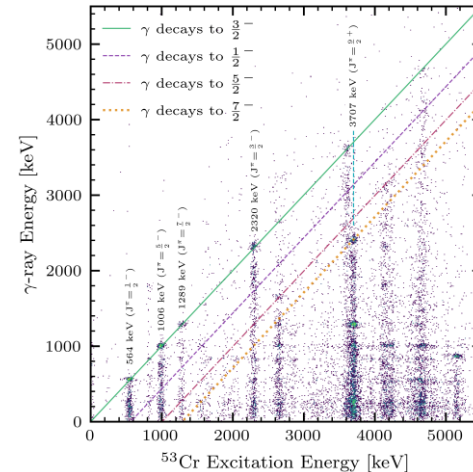
## How to search for $vg_{9/2}$ strength with greater sensitivity

- Use the  $(\alpha, {}^3\text{He})$  reaction

${}^{51}\text{V}(\alpha, {}^3\text{He}){}^{52}\text{V}$  at 32 MeV: Incoming  $\alpha$  and outgoing  ${}^3\text{He}$  differ in  $L$  by  $6.8\hbar$ .

${}^{51}\text{V}(d, p){}^{52}\text{V}$  at 16 MeV: Incoming  $d$  and outgoing  $p$  differ in  $L$  by  $1.1\hbar$ .

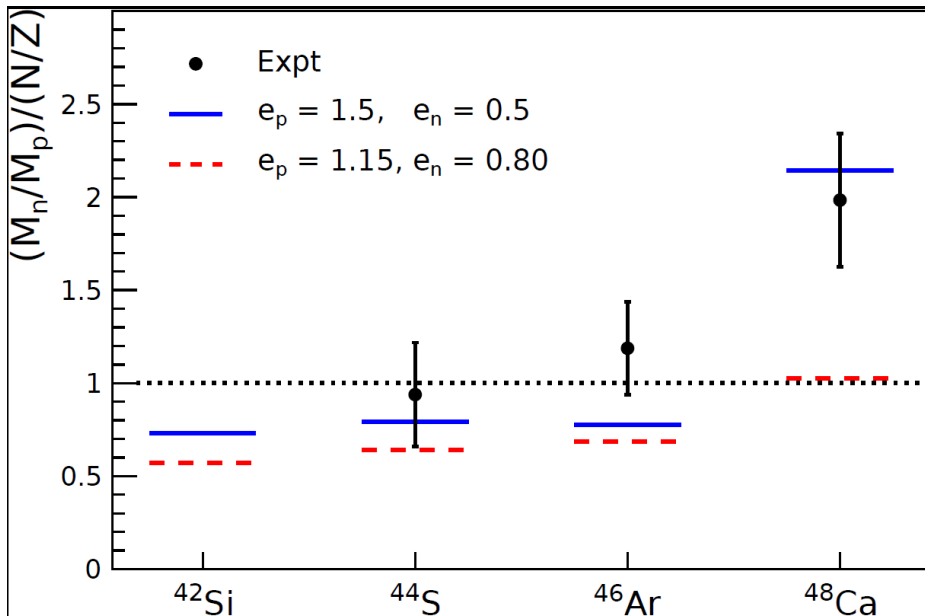
- Particle- $\gamma$  coincidences with CeBrA.



- Work on pinning down  $J^\pi$  assignments using particle- $\gamma$  coincidences and the  $^{49}\text{Ti}(t,p)^{51}\text{Ti}$  reaction to reduce uncertainties in single neutron energies.
- Hunt for missing  $vg_{9/2}$  strength using  $(\alpha, ^3\text{He})$  reactions and particle- $\gamma$  coincidences.



# Postscript: $M_n/M_p$ in $^{42}\text{Si}$ via Coulex and $(p,p')$ – FRIB expt 21001



Ursinus/FSU/MSU collaboration  
(PDC co-spokesperson)

Coulex measurement completed  
summer 2023 (being analyzed).

$(p,p')$  scheduled for late March 2024.

L.A. Riley *et al.*, Phys. Rev. C 100, 044312 (2019).

